

## chain-consistent-continuity2<sup>13,45</sup>

$\forall es:\text{ES}, Cmd:\text{Type}, In:\text{AbsInterface}(Cmd), isupdate:(Cmd \rightarrow \mathbb{B}), Sys, Out:\text{AbsInterface}(\text{Top}).$   
 $(E(In) \subseteq_r E(Sys))$   
 $\Rightarrow (\forall f:\text{sys-antecedent}(es; Sys).$   
 $(\forall e:E(In). f(e) = e \in E)$   
 $\Rightarrow (\forall chain:(E(Sys) \rightarrow (\text{Id List})).$   
 $\quad \text{chain-consistent}(f; chain)$   
 $\Rightarrow (\forall x, y:E(Sys).$   
 $\quad x \text{ is } f*(y)$   
 $\Rightarrow (\forall z:E(Sys).$   
 $\quad y \leq_{\text{loc}} z$   
 $\Rightarrow \text{loc}(x) <<= \text{loc}(f(z))$   
 $\Rightarrow (\exists e:E(Sys). (\text{loc}(e) = \text{loc}(f(z)) \in \text{Id} \& e \text{ is } f*(y) \& x \text{ is } f*(e))))))$